



Fermi National Accelerator Laboratory

TM-1490

Tracking Results Using a Standard Cell Lattice

Norman M. Gelfand
Fermi National Accelerator Laboratory
P.O. Box 500, Batavia, Illinois 60510

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This is a summary of results obtained by tracking a single particle through a lattice composed of a r.f. cavity and standard FODO cells. The lattice also includes two families of sextupoles for controlling the chromaticity. The parameters of the cells, i.e. their length and phase advance, closely resemble those of the Fermilab Main Ring or the Tevatron. We therefore have a model lattice which is similar to that of those accelerators but without the straight sections present in the actual machines. It is hoped that the simplified model used will exhibit the salient features of the actual accelerator but will be simpler to understand.

The model machine contains 774 dipoles (the number in the Tevatron) and the high order multipoles ($n > 1$) measured at the Fermilab MTF for the Tevatron magnets were used in the tracking calculations. The exclusion of the measured skew quadrupole moments of the dipoles means that there is no linear coupling in our model. The Tevatron magnets have fields that fall off sharply at a radius of approximately 1 in. This shape is peculiar to the Tevatron magnets (as well as any other "cos theta" magnets) and to study more general kinds of behavior it would not be desirable to have

this sharp fall off. For this reason only the measured sextupole and octupole (both normal and skew) moments were used in the tracking.

The ordering of the magnets in the lattice determines the strength of the harmonic driving terms. The ordering used for the nominal case corresponds to the "shuffled" order used in the actual Tevatron where the magnets are positioned in the lattice to reduce several of the low order driving terms.

I. Fourier Transform Analysis

In the tracking code (Tevlat) a particle was placed at an initial point in phase space and with an initial value of dp/p and was tracked around the test lattice. As the particle returned to the starting point the current phase space coordinates were recorded. Thus a turn (or alternately a time) sequence of phase space coordinates was developed. The Fourier transform of this sequence was computed using a fft routine to determine the tune spectrum of the motion. Figure 1 shows the spectrum in the case where the initial dp/p was 0.0% and without synchrotron oscillations. The sextupole families were set to give the lattice zero chromaticity. The spectrum is rich. There are components corresponding to the linear tunes in x and y as well as harmonic components corresponding to the non-linear contributions from the sextupole and octupole moments.

In the tracking code the values of both x and x' are available at the end of each turn. With (x, x') and a knowledge of the values of beta and alpha at the starting point the x amplitude $(= (x^2 + (\beta_x x' + \alpha_x x)^2)^{1/2}$ can be calculated at the end of each turn. If this were simply a linear lattice, without coupling the amplitude would be the same turn to turn. The variation of the amplitude therefore reflects the deviation from the simple linear machine. The x and y amplitudes, as a function of turn, are plotted in Figure 2a. Also plotted in Figure 2a is the square root of the sum of the squares of the x and y amplitudes. The amplitudes are obviously not constant. The Fourier transform (Figure 2b) of the amplitude shows the same frequencies are present in the amplitudes as are present in the coordinates. This is not surprising. What is interesting and possibly useful, in studying the behavior of a real machine, is that the amplitudes of the linear tunes are much smaller relative to the other lines than when the coordinates are analyzed.

In addition to the lines corresponding to the harmonics of the tunes and the non-linear elements seen in the fourier transform of the coordinates there is also very obviously a very long period oscillation of the amplitude.

The question naturally arises whether the particular behavior seen, particularly of the amplitudes, is simply due to the ordering of the magnets or is a more general feature of the model. Accordingly the order of the magnets was permuted and the tracking was repeated. The amplitude is plotted as a function of turn for 10 permutations (Figure 3). The distributions certainly differ. There is also apparent in several of the distributions, the long period oscillation in the amplitudes seen in our original ordering. The period of these very slow oscillations differs from the permutation to the next and is therefore not likely to be due to the structure of the lattice but instead it reflects the ordering of the magnets. The lines in the fourier transforms of these amplitude-turn distributions have similar positions but the strength of the lines differ.

The long term oscillations are an unexpected result of the tracking for which no explanation was obvious to me. The tracking was therefore repeated first only the sextupole moments and then only with the octupole moments. When the amplitudes from the case with only sextupoles (Figure 4) are studied no long term oscillations are apparent. For the amplitudes, in the case where the only high order moments are the octupole moments (Figure 5a), there is a suggestion of a long term oscillation with ever a greater period than

before. It is crucial to recognize that these last tracking results were obtained with the chromaticity sextupoles adjusted to give zero chromaticity. When the tracking is repeated with the chromaticity sextupoles turned off (the lattice now has its natural chromaticity of $c_x \sim -20$, $c_y \sim -20$) there is no suggestion of a long term oscillation (Figure 5b). I feel it is proper at this point to conclude that the long term oscillation is the result of interaction between the sextupole and octupole moments in the lattice.

The effect of the synchrotron oscillations on the motion has been studied. Figure 6a shows the amplitude variation in the case of an off momentum particle and with synchrotron oscillations. There is a long period variation in the amplitudes in this situation too. The variation in the x and y amplitudes, both with and without synchrotron oscillations, seem to be "in phase". The distributions in Figure 6a are with the chromaticity sextupoles set to give zero chromaticity. Since we have seen that the long term oscillations are sensitive to the strength of these sextupoles I have varied them by instructing the program to set the chromaticity to $c_x = +10.0$, $c_y = -10.0$. The tracking was then repeated. In general the distributions are similar to those with zero chromaticity (Figure 6b) but the distribution resulting from the sixth permutation is

anomalous showing a change in the amplitude and in the period of the long term oscillation after approximately 1000 turns (Figure 6c).

The details of the amplitude variation depend not only on the ordering of the magnets but also on the initial point in phase space at which we start the tracking. Figures 7a-f are plots of the amplitudes, using the ordering of the magnets of permutation #6, with the chromaticity $c_x = 10$, $c_y = -10$, for six different initial values for (x, x') , all of which have the same x amplitude. Both the period and the size of the amplitude variations change with the different starting points. If we reduce the initial displacement from 7 mm to 6 mm the long term oscillation of the amplitude disappears (Figures 8a-f).

An attempt has been made to calculate the driving terms for the nominal distribution, the anomalous distribution (permutation #6) and for the 1000 random distributions in the hope that one could recognize some property of permutation #6 which would enable one to identify potentially troublesome orderings of magnets. The driving terms from both the sextupole and octupole moments for permutation #6 appear similar to those of the nominal distribution (though, as would be expected, slightly larger in magnitude) but quite typical of the driving terms

calculated from the 1000 random permutations. I would therefore conclude that the driving terms will not be useful in predicting the kind of behavior seen in Figure 3f.

In summary the tracking calculations show unexpected behavior in the amplitudes. These are characterized by long term, apparently periodic, variations in the amplitudes. These variations, both in size and period, depend critically on the initial conditions (being far more prominent at large amplitudes) and on the ordering of the moments in the lattice. I do not have a good understanding of the source of these oscillations but they apparently arise from a conspiracy between the sextupole and octupole moments. The nature of the oscillations also depends on the synchrotron motion.

TABLE I

Nominal Tunes Used:

$$\nu\text{-}x = 19.42123$$

$$\nu\text{-}y = 19.38123$$

Lattice properties at the starting point of the tracking

$$\beta\text{ }x = 97.3 \text{ m}$$

$$\beta\text{ }y = 29.2 \text{ m}$$

$$\alpha\text{ }x = -1.87$$

$$\alpha\text{ }y = +0.59$$

r.f. characteristics:

$$\text{harmonic number (h)} = 1113$$

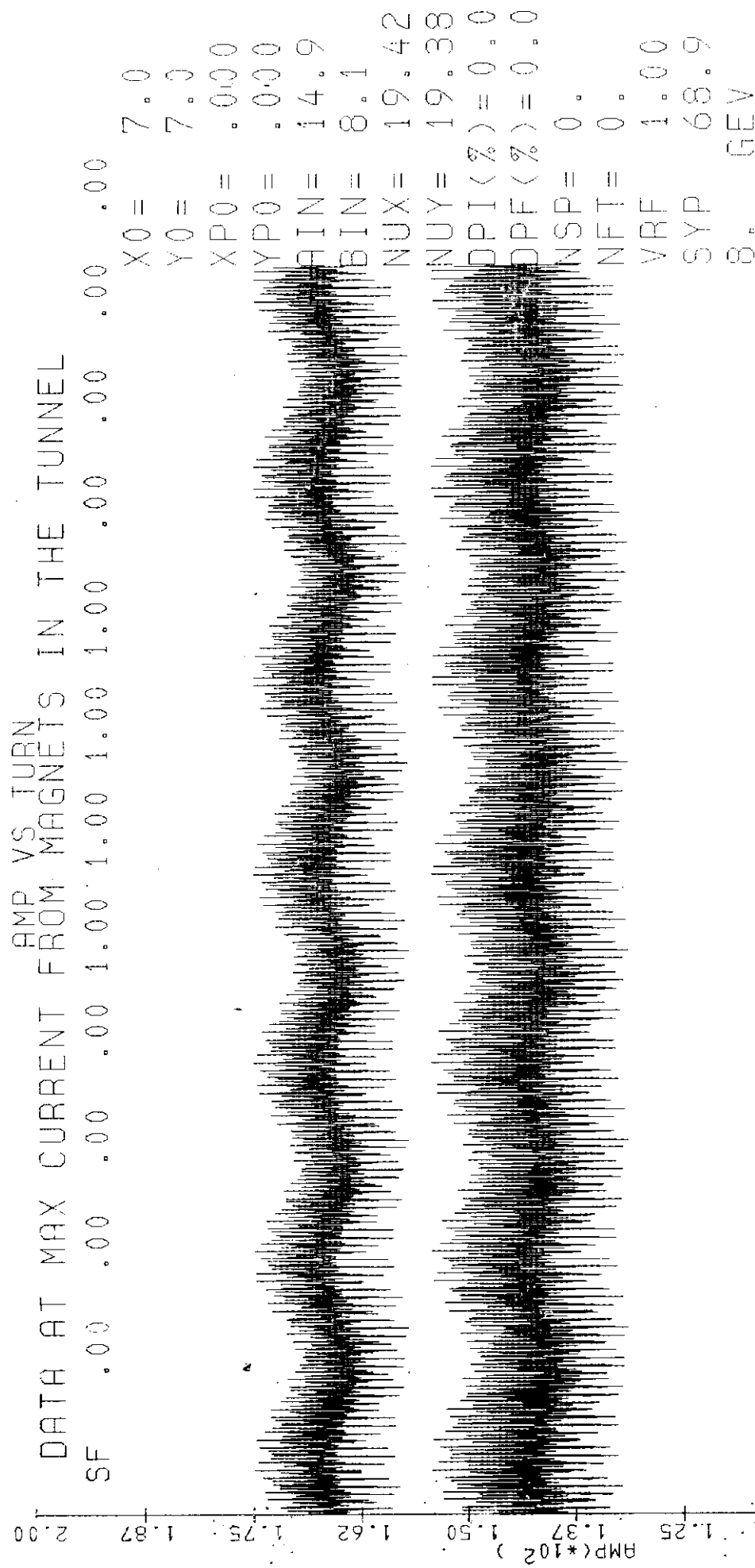
$$\text{r.f. phase angle} = 30 \text{ deg}$$

$$\text{transition gamma} = 18.4$$

$$\text{compaction factor (8 GeV)} = -0.00108$$

Figure Captions

- Figure 1 Amplitude of the Fourier transform of the coordinates. Several of the lines present in the transform of the x coordinate are identified.
- Figure 2 (a) The amplitude as a function of turn for the nominal ordering of the moments.
(b) The amplitude of the Fourier transform of the x amplitude.
- Figure 3 (a)-(j) The amplitude as a function of turn for ten permutations of the order of the moments.
- Figure 4 The amplitude as a function of turn with only sextupole magnets.
- Figure 5 (a) The amplitude as a function of turn with only octupole magnets, $c_x = c_y = 0.0$.
(b) The amplitude as a function of turn with only octupole magnets, $c_x \sim c_y \sim 20$.
- Figure 6 (a) The amplitude as a function of turn with synchrotron oscillations with $c_x = c_y = 0.0$. Nominal distribution.
(b) The amplitude as function of turn with synchrotron oscillations with $c_x = +10.0$, $c_y = -10.0$. Nominal distribution.
(c) The amplitude as function of turn with synchrotron oscillations with $c_x = c_y = 0.0$. Permutation #6.
- Figure 7 (a)-(f) The amplitude as a function of turn for the ordering of permutation #6 but with different initial coordinates in phase space. The initial displacement is 7 mm for x and y.
- Figure 8 (a)-(f) The amplitude as a function of turn for the ordering of permutation #6 but with different initial coordinates in phase space. The initial displacement is 6 mm for x and y.



86/12/18. 09.08.3
 86/12/18. 10.01.3
 TC11C FILE 1.

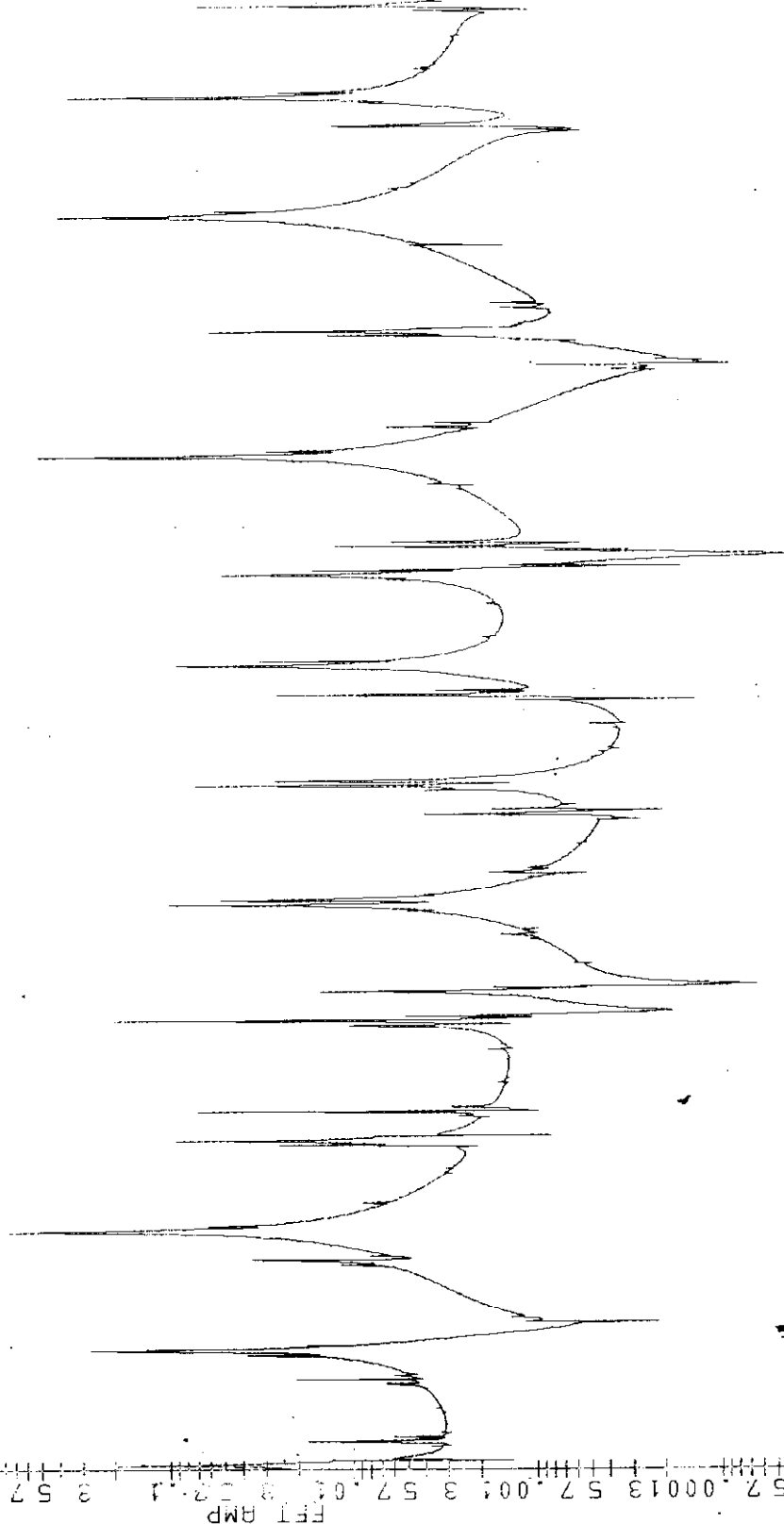
0.00 .40 .81 1.22 1.63 2.04 2.45 2.86 3.27 3.68 4.00
 TURN(*10⁻³)

FIG.2a

FOURIER TRANSFORM OF X AMP FROM TEVL DATA AT MAX CURRENT FROM MAGNETS IN THE TUNNEL

SF .00 .00 .00 .00 1.00 1.00 1.00 1.00 .00 .00 .00 .00

X0 = 7.0
Y0 = 7.0
XP0 = .000
YP0 = .000
AIN = 14.9
BIN = 8.1
NUX = 19.42
NUY = 19.38
DPI(%) = 0.0
DPF(%) = 0.0
NSP = 4097.
NFT = 4096.
VRF = 1.00
SYP = 68.9
8. GEV



86/12/18. 09.08.3
86/12/18. 10.01.3
TC11C FILE 1.

NUM = 14.

FIG.2b

2.00 T DATA AT MAX CURRENT FROM AMP VS TURN MAGNETS IN THE TUNNEL

AMP VS TURBID

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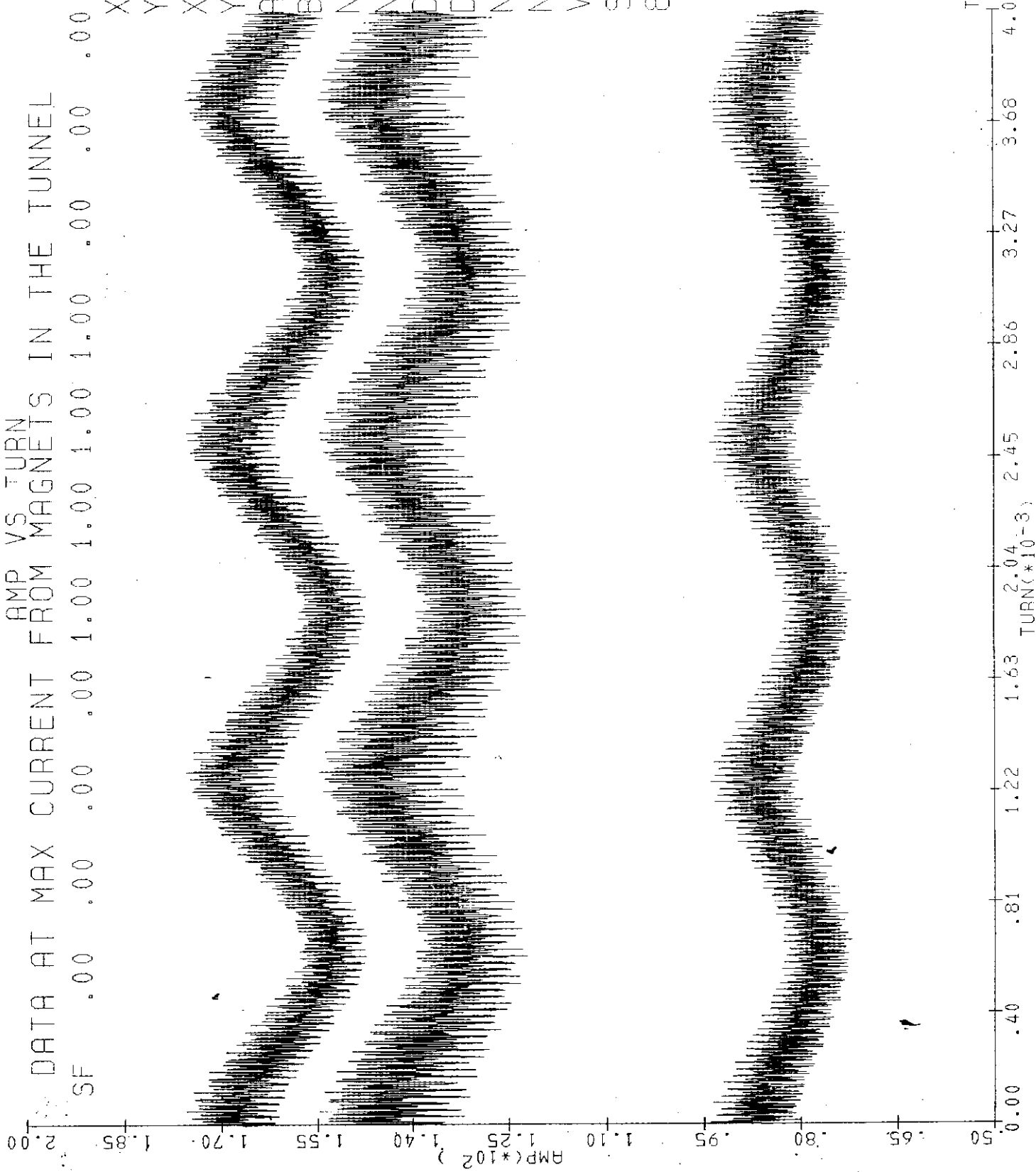
2761 XIX = 1942

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[illegible][illegible]

86/12/18. 09.11.11
86/12/18. 10.01.13
UC11C FILE 2.

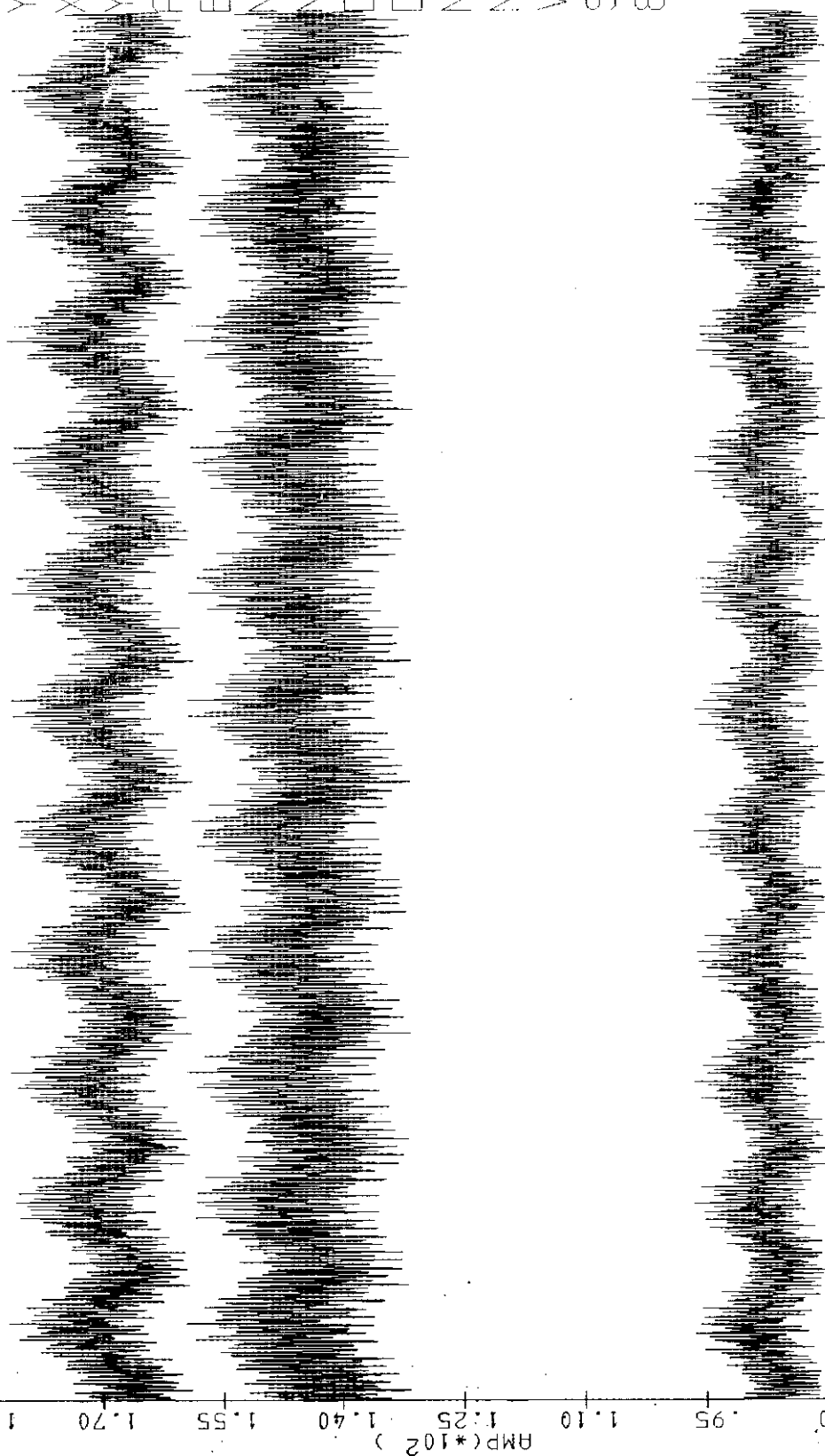
— $\text{AUM} = 15$.

FIG. 3a

DATA AT MAX CURRENT FROM MAGNETS IN THE TUNNEL

SF .00 .00 .00 .00 1.00 1.00 1.00 1.00 .00 .00 .00 .00

X0 = 7.0
Y0 = 7.0
XP0 = .000
YP0 = .000
AIN = 14.9
BIN = 8.1
NUX = 19.42
NUY = 19.38
DPI(%) = 0.0
DPF(%) = 0.0
NSP = 0.
NFT = 0.
VRF = 1.00
SYP = 68.9
8. GEV



86/12/18. 09.14.2
86/12/18. 10.01.3
TC11C FILE 3.

NUM=18.

FIG.3b

DATA AT MAX CURRENT FROM MAGNETS IN THE TUNNEL

SF .00 .00 .00 .00 1.00 1.00 1.00 1.00 .00 .00 .00 .00

X0 = 7.0
Y0 = 7.0
XP0 = .000
YP0 = .000
AIN = 14.9
BIN = 8.1
NIX = 19.42
NIY = 19.38
DPI (%) = 0.0
DPF (%) = 0.0
NSP = 0.
NFT = 0.
VRF 1.00
SYP 68.9
8. GEV

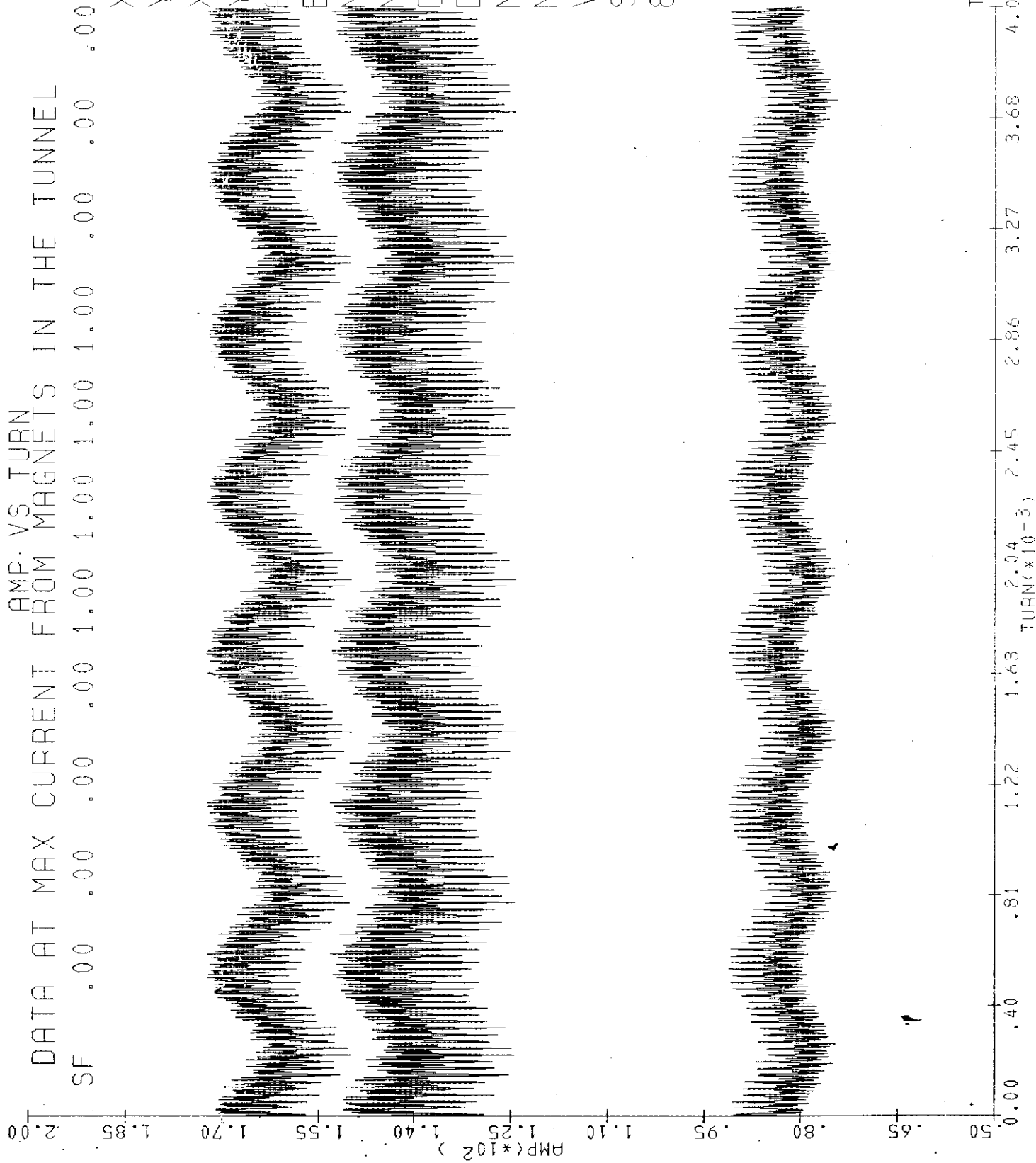
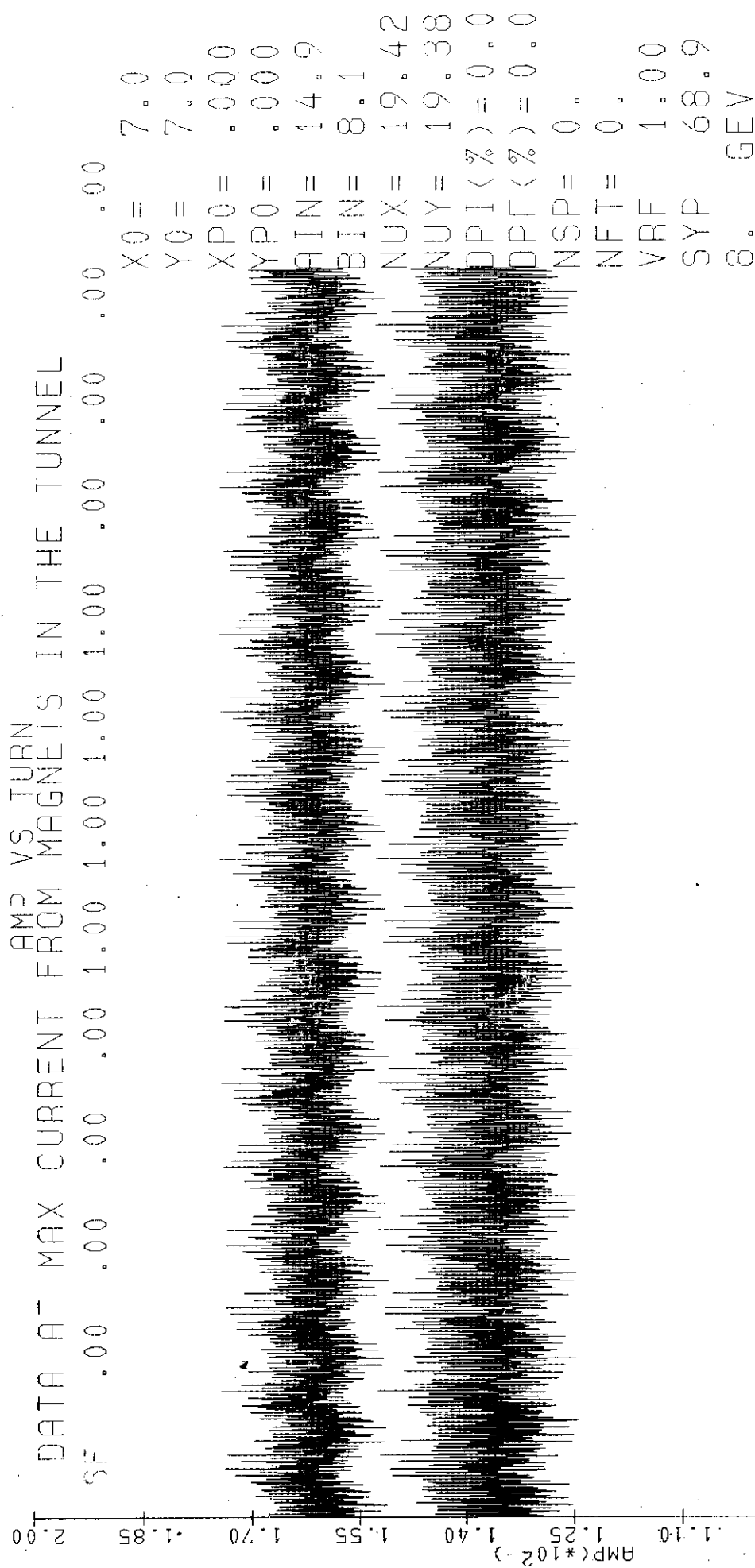


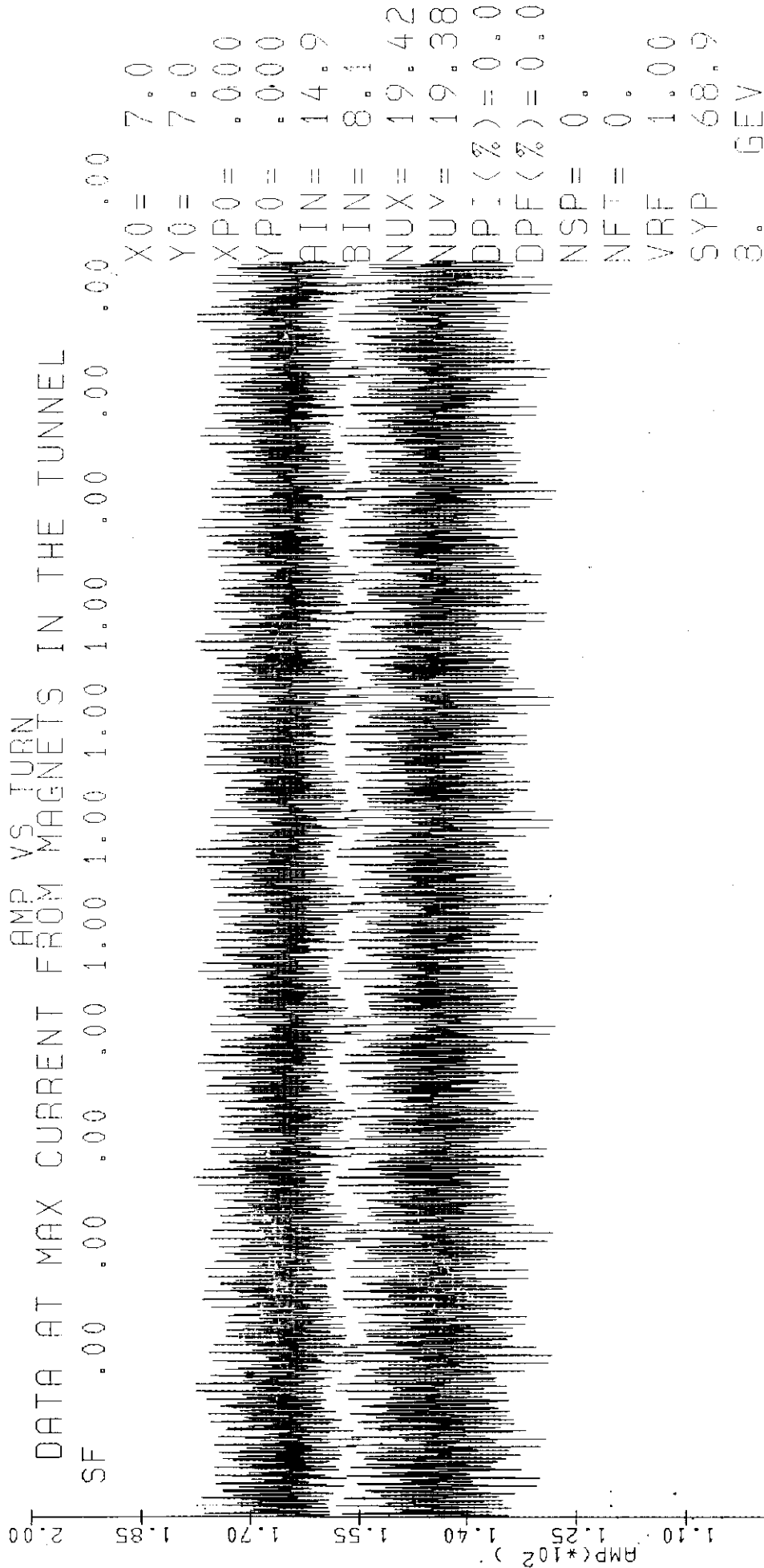
FIG.3c



86/12/18. 09.19.4
 86/12/18. 10.01.3
 TC11C FILE 5.

NUM=24.

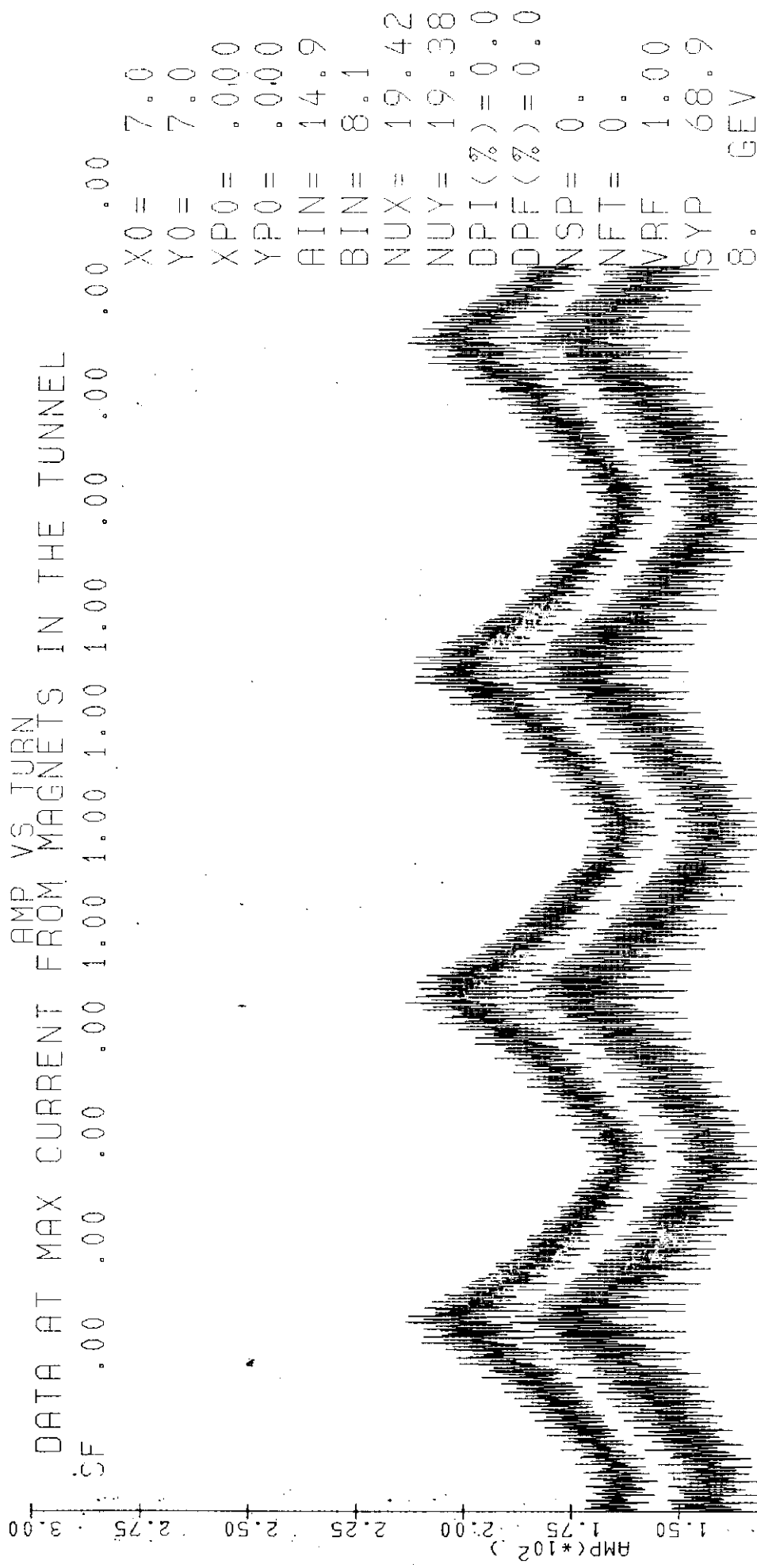
FIG. 3d



85/12/18. 09.22.3
 86/12/18. 10.01.3
 TC11C FILE 6.

NUM= 27.

FIG. 3e



86/12/18. 09.25.4
 86/12/18. 10.01.3
 TC11C FILE 7.

NUM=30.
 TURN(*10⁻³) 0.40 0.81 1.22 1.63 2.04 2.45 2.86 3.27 3.68 4.00

FIG.3f

DATA AT MAX CURRENT FROM MAGNETS IN THE TUNNEL

SF .00 .00 .00 .00 1.00 1.00 1.00 1.00 .00 .00 .00 .00

X0 = 7.0

Y0 = 7.0

XP0 = .000

YP0 = .000

AIN = 14.9

BIN = 8.1

NUX = 19.42

NUY = 19.38

DPI (%) = 0.0

DPF (%) = 0.0

NSP = 0.

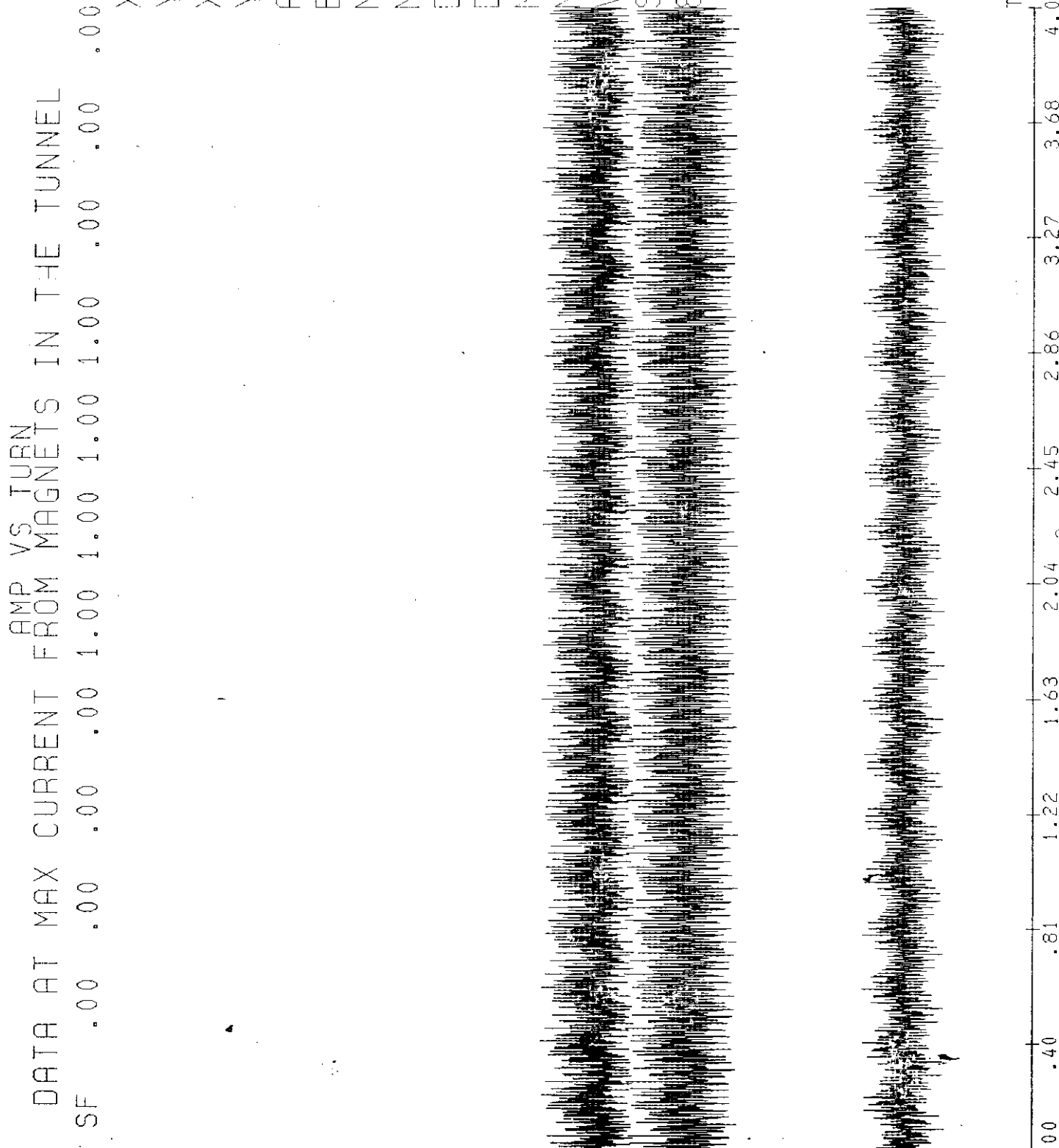
NET = 0.

VRF = 1.00

SYP = 68.9

8. GEV

AMP(*10²)



TURN(*10⁻³)

TC11C

NUM=36.

FIG. 3h

86/12/18. 09.32.3

86/12/18. 10.01.3

FILE 9.

DATA AT MAX CURRENT FROM MAGNETS IN THE TUNNEL

SF .00 .00 .00 .00 1.00 1.00 1.00 1.00 .00 .00 .00 .00

X0 = 7.0

Y0 = 7.0

XPO = .000

YPO = .000

AIN = 14.9

BIN = 8.1

NUX = 19.42

NUY = 19.38

DPI (%) = 0.0

DPF (%) = 0.0

NSP = 0.

NFT = 0.

VRF = 1.00

SYP = 68.9

S. GEV

AMP(*10²)







86/12/13. 09.38.1
86/12/13. 10.01.3
TC11C FILE 11
NUM = 42.

TURN(*10⁻³)

FIG. 3j

DATA AT MAX CURRENT FROM AMP VS TURN IN THE TUNNEL

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$$Y = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

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U.S. DEPARTMENT OF JUSTICE

87/01/0

87/01/0

NUM=12.

7.

FIG. 4

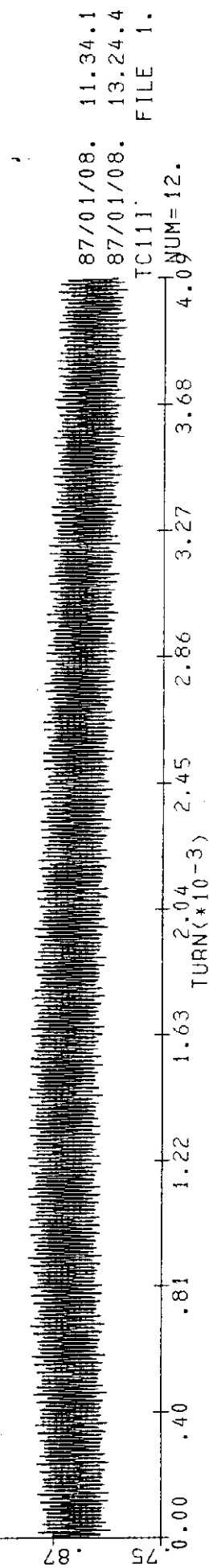
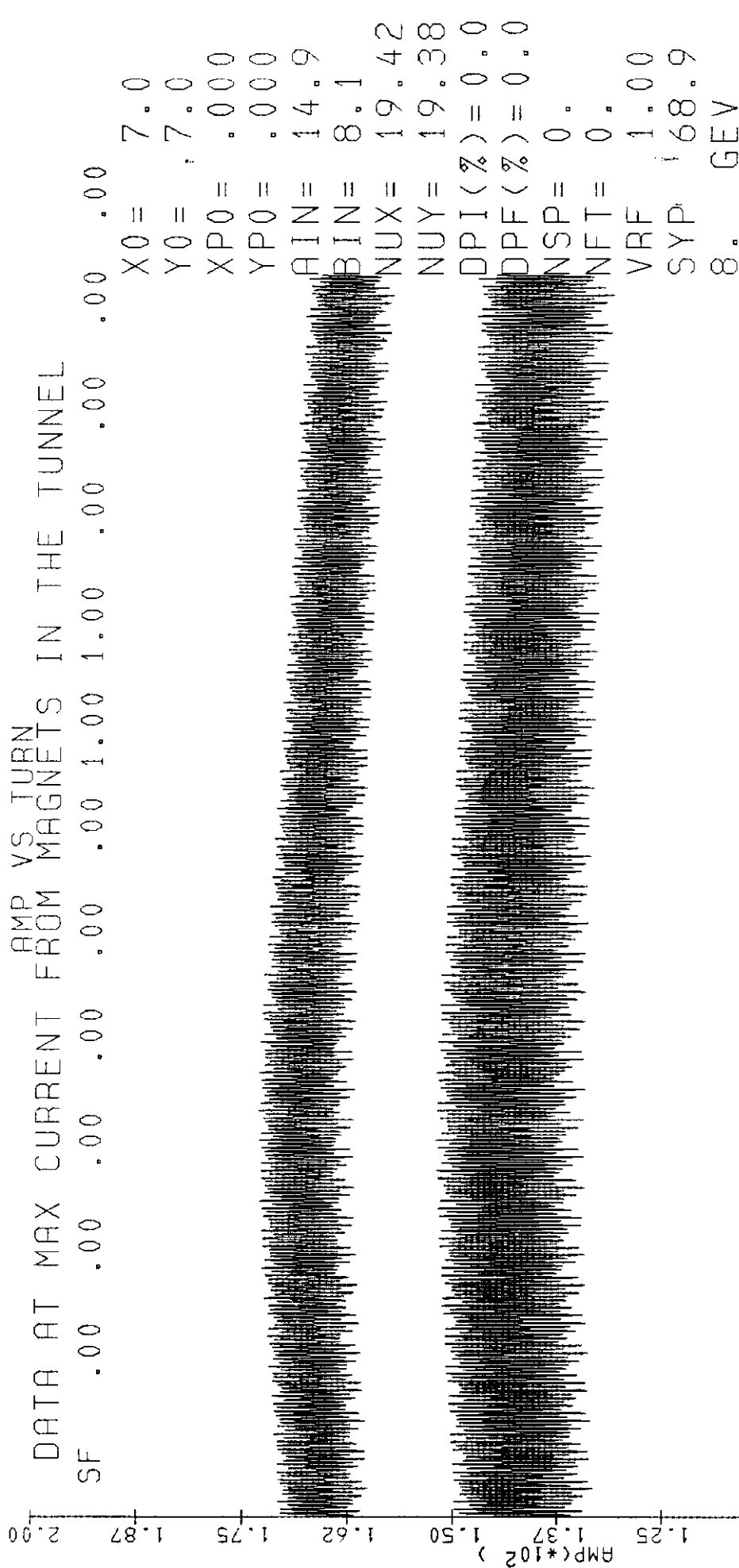
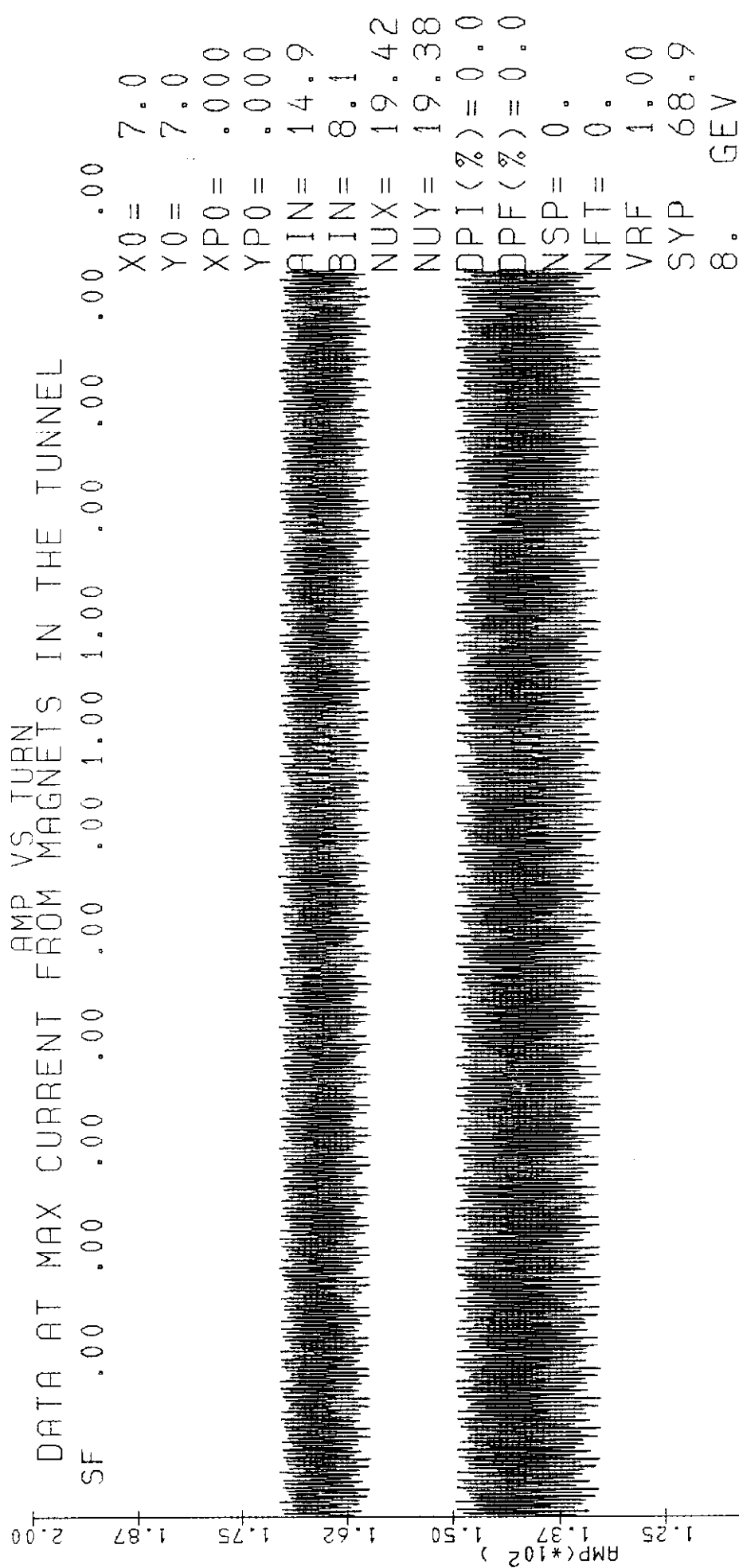


FIG.5a



87/01/09. 15.09.4
87/01/09. 16.21.4
TC11K
FILE 1.

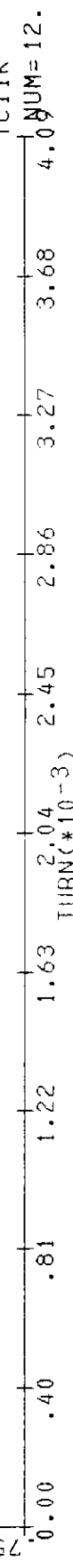


FIG.5b

DATA AT MAX CURRENT FROM AMP VS TURN MAGNETS IN THE TUNNEL

SF

	a.	b.	c.	d.	e.	f.
0.00	0.00	0.00	0.00	1.00	1.00	0.00
0.00	0.00	0.00	1.00	1.00	1.00	0.00
0.00	0.00	0.00	0.00	0.00	0.00	0.00

$$Z = 0$$

\square

$$\|YPO\| = 0.000$$

14.9

$$NUX = 19.42$$

8364 YUN

DPI (%) = 0.2

DPF (%)

011652

$$\mathbf{Z}^T = \mathbf{0}$$

VERIFIED

SYD 68.9

800 GEV

86/12/18. 10.51.0

86%.12/18. 13.39.1

TC11D FILE 1.

471 = $W \cap R$.

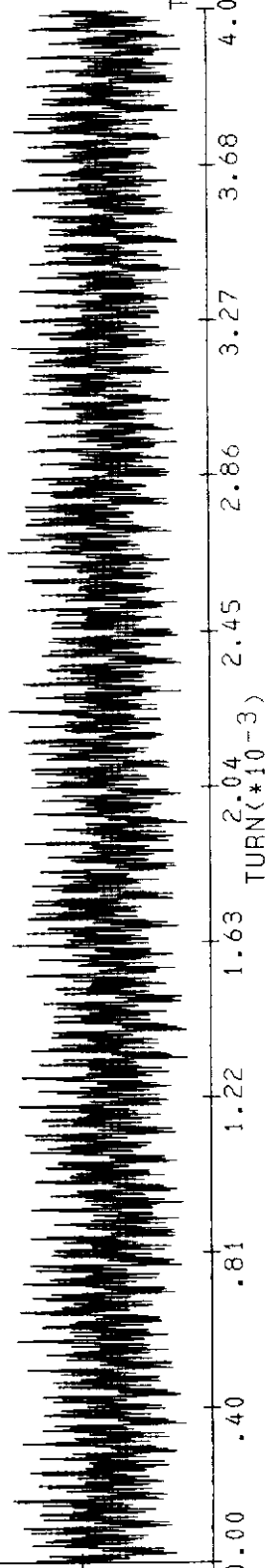
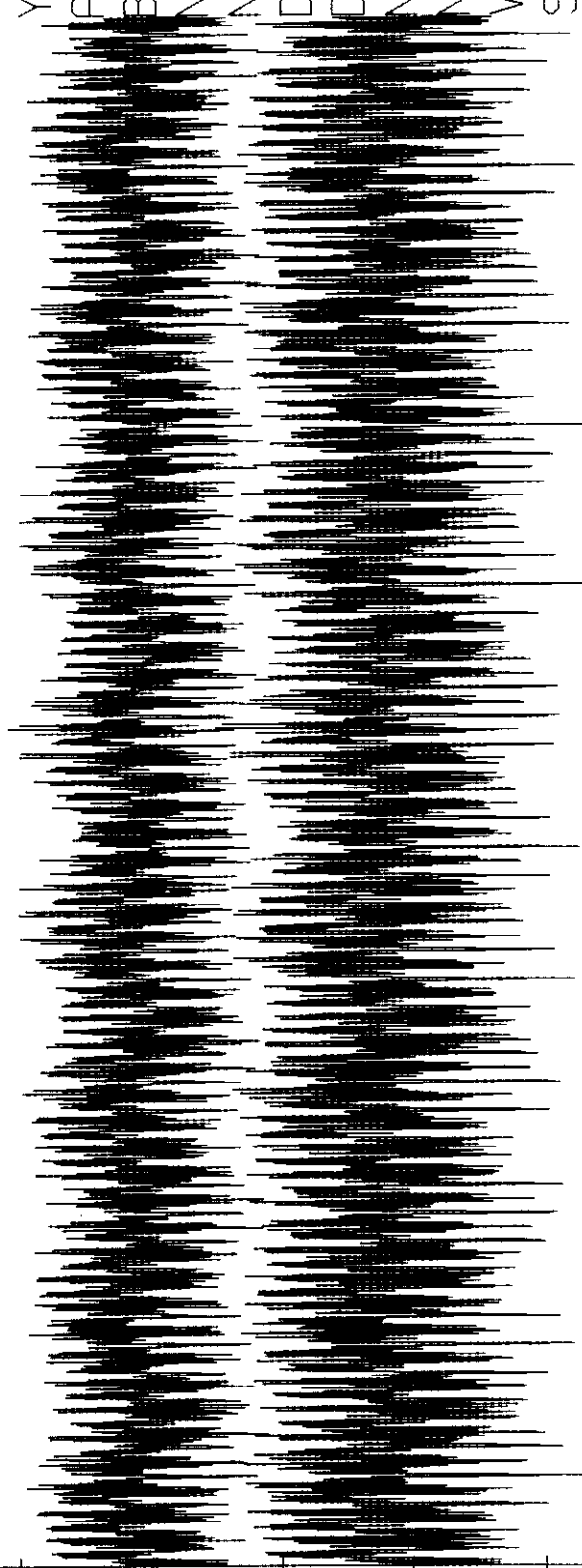
FIG. 6a

DATA AT MAX CURRENT FROM MAGNETS IN THE TUNNEL

SF .00 .00 .00 .00 1.00 1.00 1.00 1.00 .00 .00 .00 .00

X0 = 7.0
Y0 = 7.0
XP0 = .000
YP0 = .000
AIN = 14.9
BIN = 8.1
NUX = 19.42
NUY = 19.38
DPI (%) = .02
DPF (%) = .00
NSP = 0.
NFT = 0.
VRF 1.00
SYP 68.9
8. GEV

AMP(*10²)



86/12/19. 08.20.2
86/12/19. 11.14.1
TC11F
FILE 1.

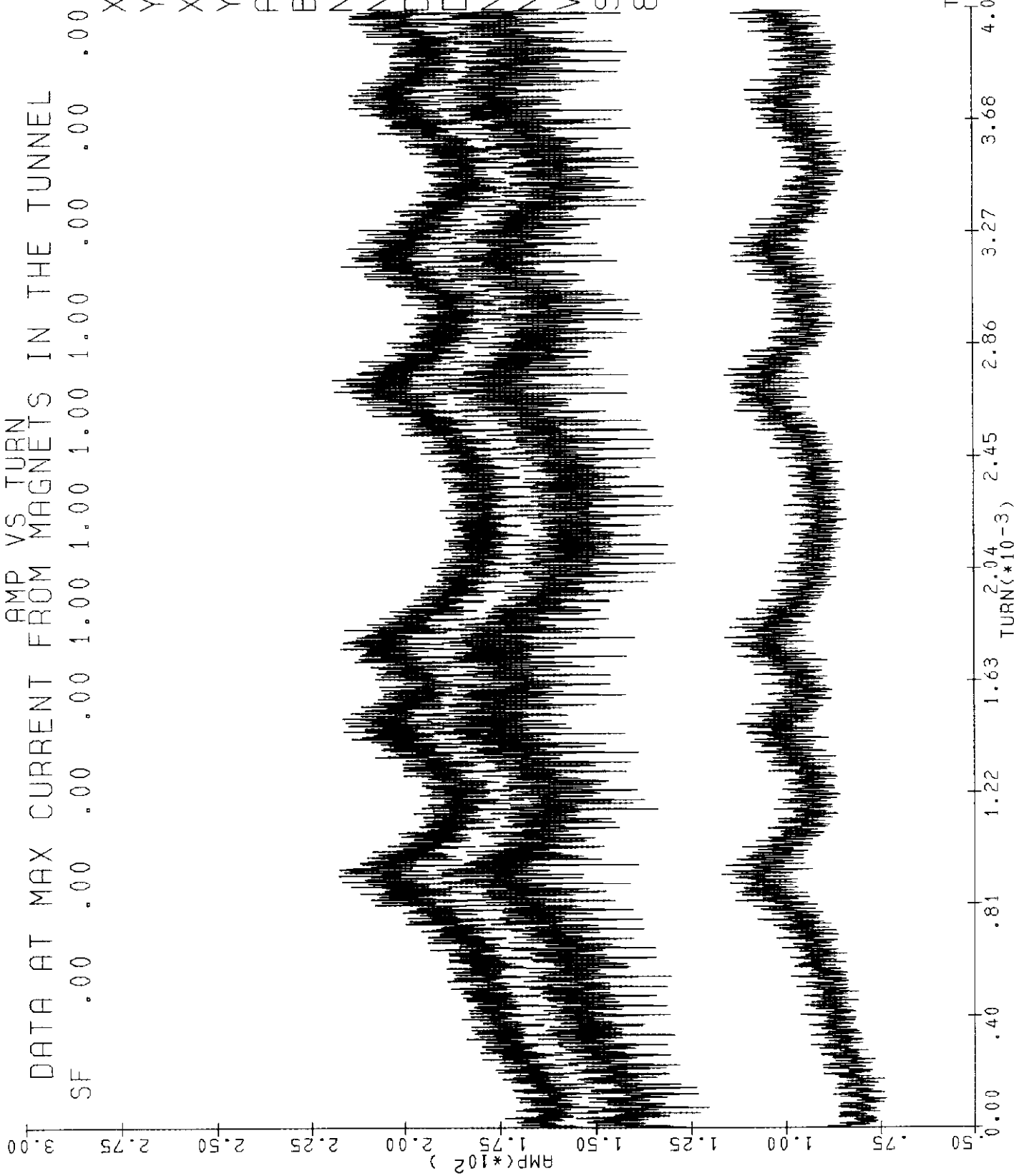
NUM=14.

FIG.6b

DATA AT MAX CURRENT FROM MAGNETS IN THE TUNNEL

SF .00 .00 .00 .00 1.00 1.00 1.00 1.00 .00 .00 .00 .00

X0 = 7.0
Y0 = 7.0
XP0 = .000
YP0 = .000
AIN = 14.9
BIN = 8.1
NUX = 19.42
NUY = 19.38
DPI(%) = .02
DPF(%) = .00
NSP = 0.
NFT = 0.
VRF 1.00
SYP 68.9
8. GEV



86/12/19. 09.38.1
86/12/19. 11.14.1
TC11F FILE 7.

NUM = 32.

FIG.6c

z/a	B/B_0 ($\alpha=0.0$)	B/B_0 ($\alpha=0.1$)	B/B_0 ($\alpha=0.2$)	B/B_0 ($\alpha=0.3$)
0.00	1.000	1.000	1.000	1.000
0.25	0.985	0.975	0.965	0.955
0.50	0.965	0.950	0.935	0.920
0.75	0.940	0.920	0.900	0.880
1.00	0.910	0.890	0.870	0.850

[illegible]

```

X0 = 7.0
Y0 = 7.0
XP0 = .000
YP0 = .000
PIN = 14.9
BIN = 8.1
NUX = 19.42
NUY = 19.38
DPI (%) = .02
DPF (%) = .00
NSP = 0.
NFT = 0.
VRF 1.00
GYO 68.9
S.      GEV

```

37/01/22. 14.24.1
37/01/23. 08.50.3
FILE 1.

○
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FIG. 7a

COFFIN-CURRENT-VOLTAGE CHARACTERISTICS IN THE TUNNEL-BARRIER-REPLICATION NOTATION

$$149 \times 10 = 1490$$

782
||
X

941121

277 1961-1972

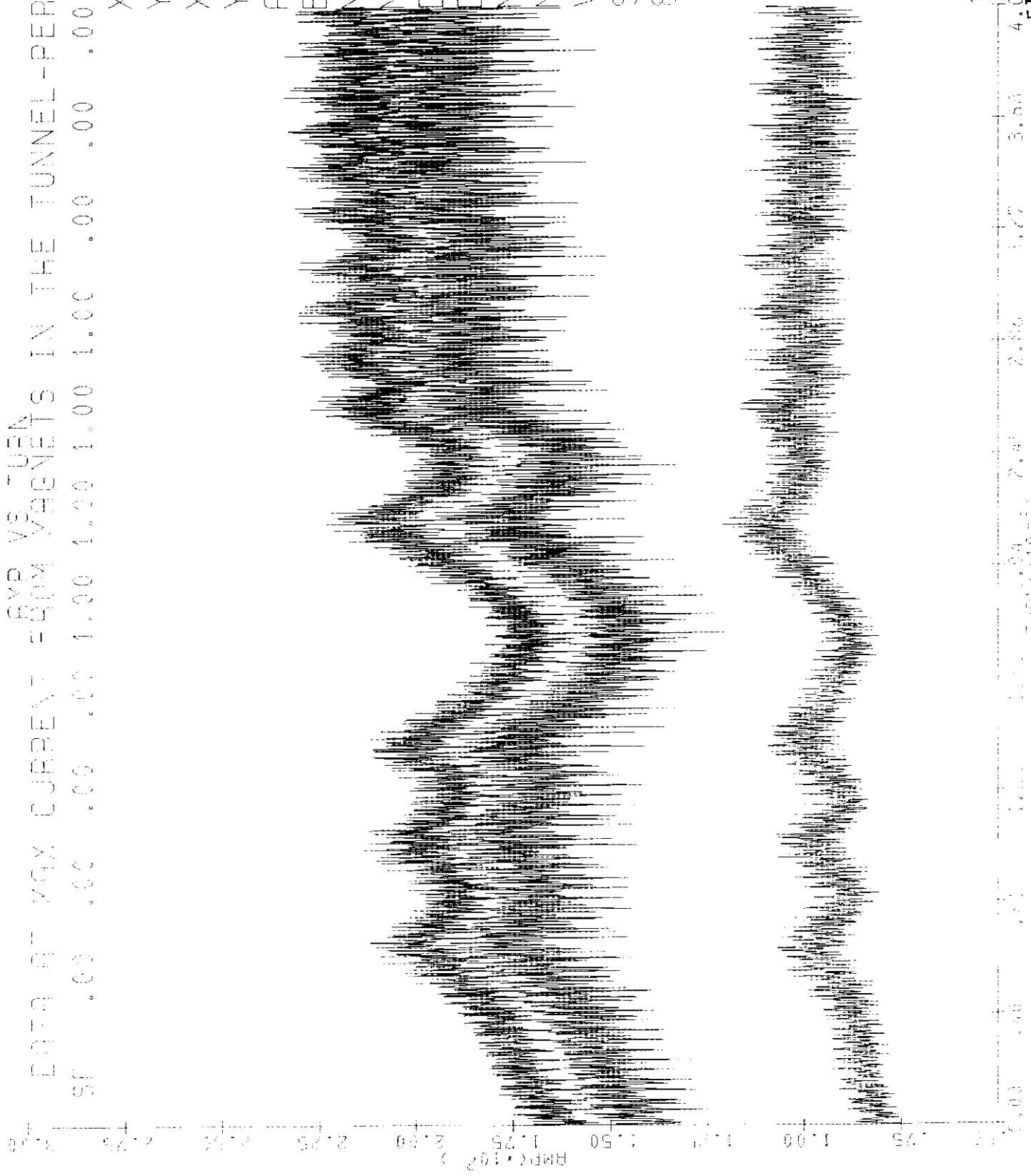
183

2011年12月26日

[illegible]

100

0
0
7
8
9

[illegible]

97/01/22. 14.24.1
87/01/23. 08.50.3
TOIN FILE 1.

2
11
22
22
T

FIG. 7b

Figure 1 is a line graph showing the variation of the average value of the normalized stress intensity factor, $K_I / (\sigma_0 \sqrt{a})$, versus the normalized crack length, a / W , for a three-point bending test. The x-axis represents a / W and ranges from 0.0 to 1.0. The y-axis represents $K_I / (\sigma_0 \sqrt{a})$ and ranges from 0.5 to 1.5. The graph shows a decreasing trend from approximately 1.4 at $a / W = 0.0$ to 0.5 at $a / W = 1.0$. Data points are plotted for different values of W/a : 1.0, 1.2, 1.5, 2.0, 2.5, 3.0, 4.0, 5.0, 6.0, 8.0, 10.0, and infinity. The curves for $W/a = 1.0, 1.2, 1.5, 2.0, 2.5, 3.0, 4.0, 5.0, 6.0, 8.0, 10.0$ are very close to each other, while the curve for $W/a = \infty$ is slightly higher.

```

Q-1 Q-2 P VBX CURRENT FROM VS TUNNEL PERMUTATION
90 .00 .00 .00 1.00 1.00 1.00 .00 .00 .00
X0= 7.9
Y0= 7.0
XP0= .28
YP0= .00
RIN= 14.
BIN= 8.1
NUX= 19.
NUY= 19.
DPI(%) = .
DPF(%) = .
NSP= 0.
NET= 0.
VRF 1.00
SYP 68.
      8. GEV

```

8701/22. 14.24.1
8701/23. 08.50.3
TCLN FILE 1.
HJUN=15.
IG.7C

4.00

2.75

2.50

2.25

2.00

1.75

1.50

1.25

1.00

.75

.50

0.00 1.00 2.00 3.00 4.00 5.00 6.00 7.00 8.00 9.00 10.00 11.00 12.00 13.00 14.00 15.00 16.00 17.00 18.00 19.00 20.00 21.00 22.00 23.00 24.00 25.00 26.00 27.00 28.00 29.00 30.00 31.00 32.00 33.00 34.00 35.00 36.00 37.00 38.00 39.00 40.00 41.00 42.00 43.00 44.00 45.00 46.00 47.00 48.00 49.00 50.00 51.00 52.00 53.00 54.00 55.00 56.00 57.00 58.00 59.00 60.00 61.00 62.00 63.00 64.00 65.00 66.00 67.00 68.00 69.00 70.00 71.00 72.00 73.00 74.00 75.00 76.00 77.00 78.00 79.00 80.00 81.00 82.00 83.00 84.00 85.00 86.00 87.00 88.00 89.00 90.00 91.00 92.00 93.00 94.00 95.00 96.00 97.00 98.00 99.00 100.00

X0 = -7.0
Y0 = 7.0
XP0 = -0.000
YP0 = 0.000
AIN = 14.9
BIN = 8.1
NUX = 19.42
NUY = 19.38
DPI(<%) = 0.02
DPF(<%) = 0.00
NSP = 0.
NFT = 0.
VRF = 1.00
SYP = 68.9
8. GEV

97/01/22. 14.24.1
97/01/23. 08.50.3
TC11N FILE 1.

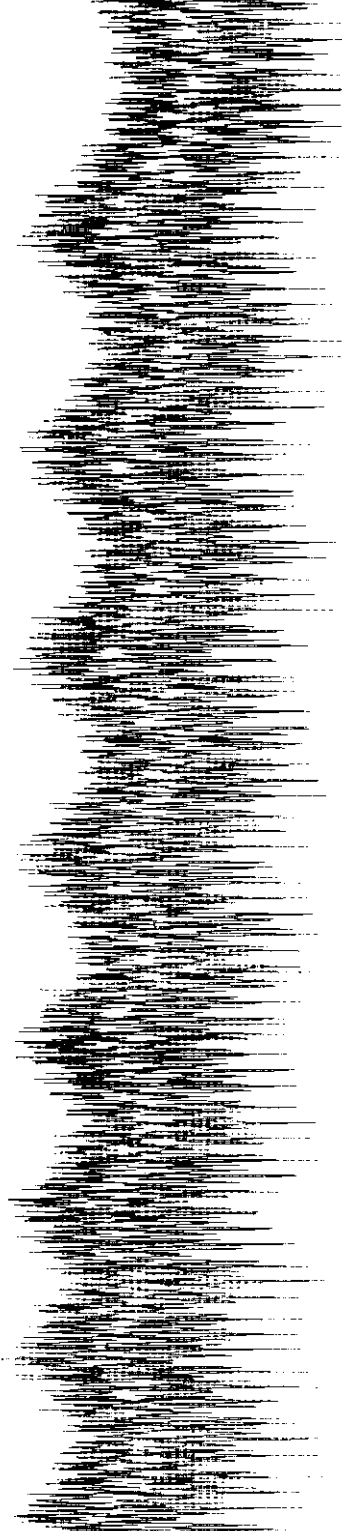
NUM=18.

FIG.7d

1.00
 .75
 .50
 .25
 .00
 AMP (x 10²)

DATA FOR MAX CURRENT FREQ VS TURN
 97 .00 .00 .00 1.00 1.00 1.00 1.00 1.00 .00 .00 .00 .00

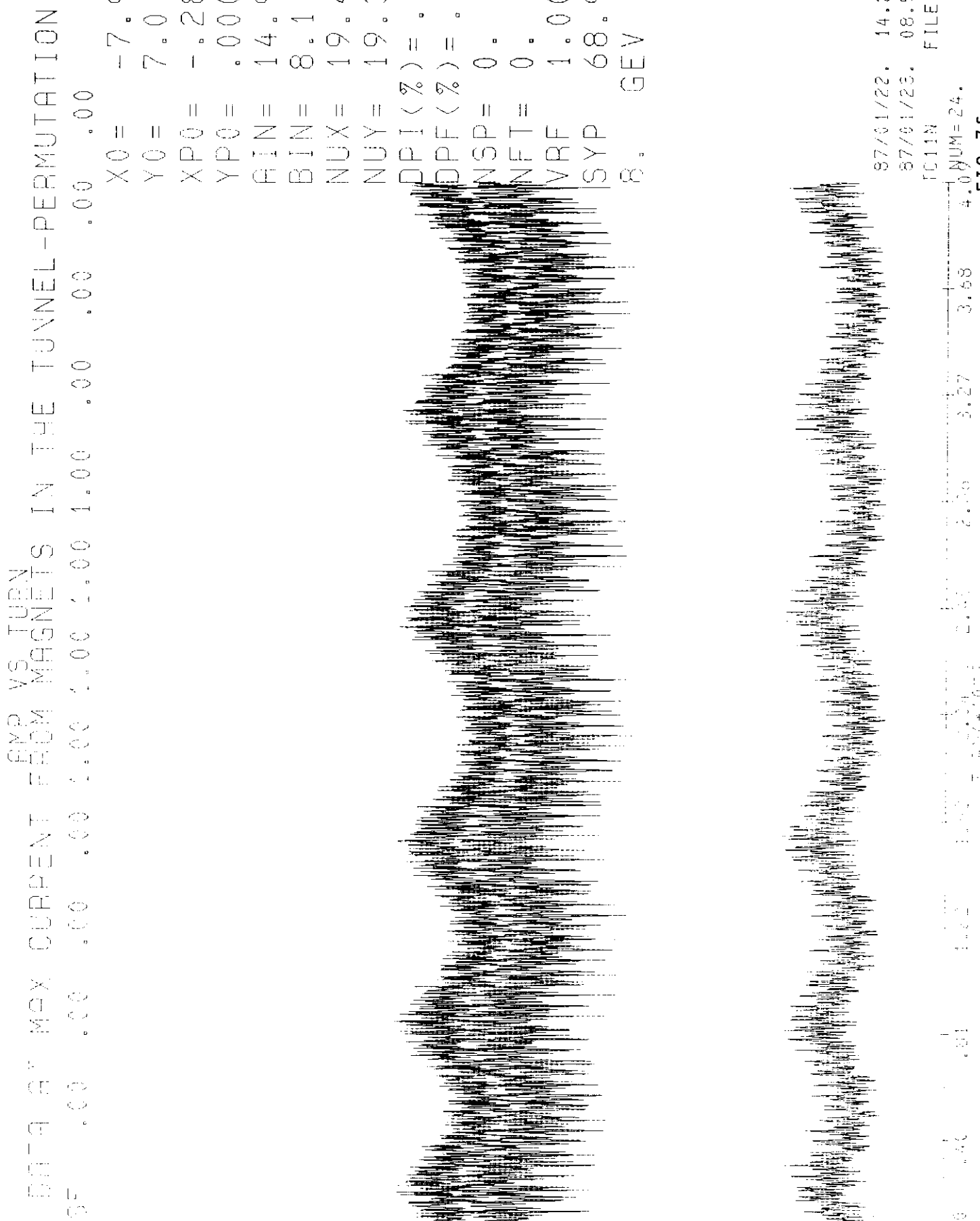
X0 = -14.9
 Y0 = 7.0
 XP0 = -.284
 YP0 = .000
 AIN = 14.9
 BIN = 8.1
 NUX = 19.42
 NUV = 19.38
 DPC (%) = .02
 DPF (%) = .00
 NSP = 0.
 NET = 0.
 VRF = 1.00
 SVP = 68.9
 8. GEV



37/01/22. 14.24.1
 87/01/23. 08.50.3
 TC11N FILE 1.
 SUM=21.

FIG.7e

0.00 0.25 0.50 0.75 1.00 1.25 1.50 1.75 2.00 2.25 2.50 2.75 3.00



DIT9 8" MAX CURRENT FROM MAGNETS IN THE TUNNEL-PERMUTATION
 SYP VS TURN
 X0 = -7.9
 Y0 = 7.0
 XP0 = -.284
 YP0 = .000
 PIN = 14.9
 BIN = 8.1
 NUX = 19.42
 NUY = 19.38
 DPI (%) = .02
 DPF (%) = .00
 NSP = 0.
 NET = 0.
 VRF = 1.00
 SYP = 68.9
 8. GEV

87/01/22. 14.24.1
 87/01/23. 08.50.3
 FC11N
 NUM=24.
 FILE 1.
 FIG.7f

2.00
1.95
1.70
1.55
1.40
1.25
1.10
.95
.80
.65
50

AMP VS TURN

DATA AT MAX CURRENT FROM MAGNETS IN THE TUNNEL-PERMUTATION

SF .00 .00 .00 .00 1.00 1.00 1.00 1.00 .00 .00 .00 .00

X0 = 6.0

Y0 = 6.0

XP0 = .000

YP0 = .000

AIN = 12.8

BIN = 6.9

NUX = 19.42

NUY = 19.38

DPI (%) = .02

DPF (%) = .00

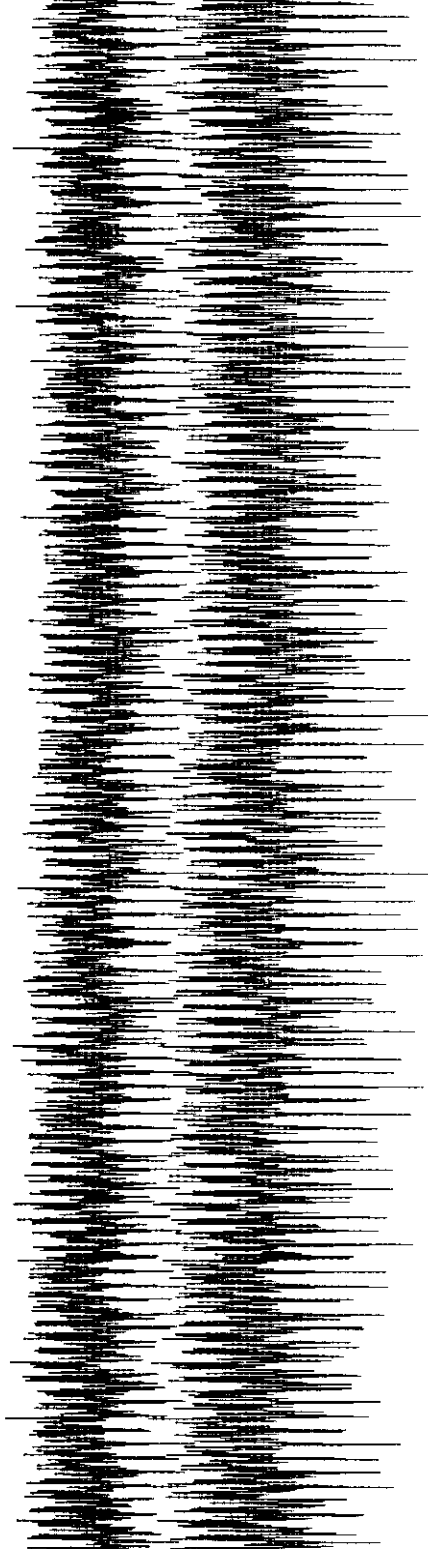
NSP = 0.

NFT = 0.

VRF 1.00

SYP 68.9

8. GEV



87/01/22. 15.42.3

87/01/23. 08.31.0

TC110 FILE 1.

NUM=9.

FIG.8a

AND VS TURN

[illegible]

[The following section contains extremely faint and illegible text, likely bleed-through from the reverse side of the page.]

1. **Introduction**
 2. **Background**
 3. **Methodology**
 4. **Results**
 5. **Discussion**
 6. **Conclusion**
 7. **References**
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 11. **Figure 3**
 12. **Figure 4**
 13. **Figure 5**
 14. **Figure 6**
 15. **Figure 7**
 16. **Figure 8**
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 213. **Figure 205**
 214. **Figure 206**
 215. **Figure 207**
 216. **Figure 208**
 217. **Figure 209**

1. The first step in the process is to identify the problem or issue that needs to be addressed. This involves gathering information and understanding the context of the problem.

1. The first step in the process is to identify the problem or issue that needs to be addressed. This involves gathering information and understanding the context of the problem.

2. Once the problem is identified, the next step is to define the objectives and goals of the project. This helps to clarify what needs to be achieved and provides a clear direction for the team.

3. The third step is to develop a plan or strategy to address the problem. This involves breaking down the problem into smaller, manageable tasks and determining the resources needed to complete each task.

4. The fourth step is to implement the plan. This involves putting the strategy into action and monitoring progress to ensure that the project is on track.

5. The final step is to evaluate the results of the project. This involves assessing the outcomes against the objectives and goals and identifying any areas for improvement.

1. The first step in the process is to identify the problem or issue that needs to be addressed. This involves gathering information and understanding the context of the problem.

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 21. *Open Access*
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 247. *References*
 248. *Appendix*
 249. <

[illegible][illegible]

0

0.50

to

2.00

1.85

1.70

1.55

1.40

1.25

1.10

.95

.80

.65

.50

RMP VS TURN

DATA AT MAX CURRENT FROM MAGNETS IN THE TUNNFL-PERMUTATION

SF .00 .00 .00 .00 1.00 1.00 1.00 1.00 1.00 .00 .00 .00 .00

X0 = 6.8

Y0 = 6.0

XP0 = .243

YP0 = .000

AIN = 12.8

BIN = 6.9

NUX = 19.42

NUY = 19.38

DPI (%) = .02

DPF (%) = .00

NSP = 0.

NFT = 0.

VRP = 1.00

SYP = 68.9

8. GEV

0.00

.40

.81

1.22

1.63

2.04

2.45

2.86

3.27

3.68

4.09

TURN(*10⁻³)

NUM = 15.

FIG.8c

87/01/22. 15.42.3

87/01/23. 08.31.0

TC110 FILE 1.

AMP(*10²)

NATIONAL BUREAU OF STANDARDS
 U.S. DEPARTMENT OF COMMERCE

DATA AT MAX CURRENT FROM MARKETS IN THE FULL PERMUTATION

SF	.00	.00	.00	1.00	1.00	1.00	1.00	1.00
SF	.00	.00	.00	1.00	1.00	1.00	1.00	1.00

```

X0 = -6.0
Y0 = 6.0
XP0 = -0.000
YP0 = 0.000
RIN = 12.8
BIN = 6.9
NUX = 19.42
NUY = 19.38
DPI (%) = .02
DPF (%) = .00
NSP = 0.
NFT = 0.
VRF 1.00
SVP 68.9
8. GEV

```



97/01/22. 15.42.3
97/01/23. 08.31.0
C110 FILE 1.

31 NORTH

88.513

AMP(*10²)

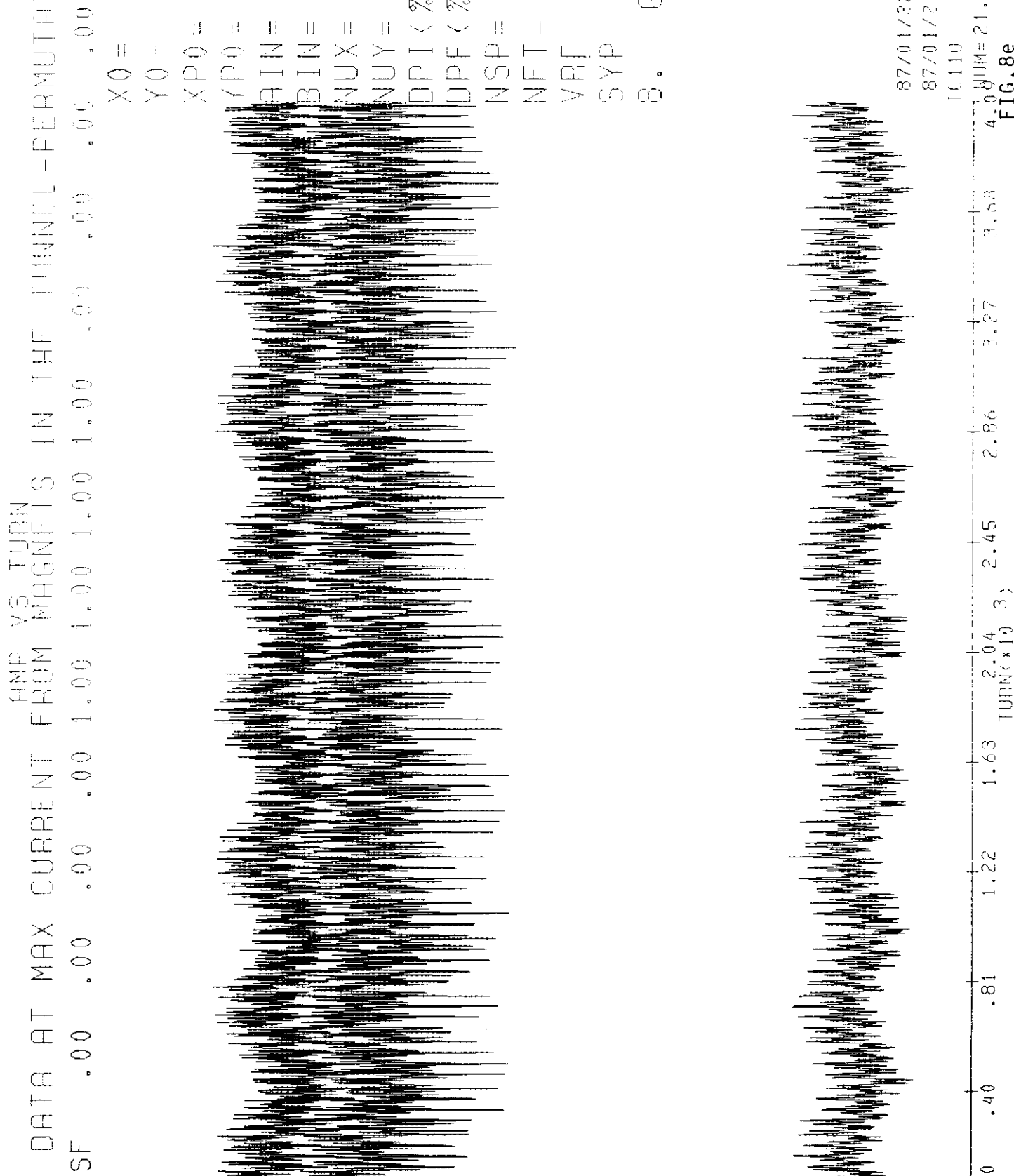


FIG.8e

DATA AT MAX CURRENT FROM MAGNETS IN THE TUNNEL

SF .00 .00 .00 .00 1.00 1.00 1.00 1.00 .00 .00 .00 .00

X0 = 7.0

Y0 = 7.0

XP0 = 0.00

YP0 = 0.00

AIN = 14.9

BIN = 8.1

NUX = 19.42

NUY = 19.38

DPI (%) = 0.0

DPF (%) = 0.0

NSP = 0.

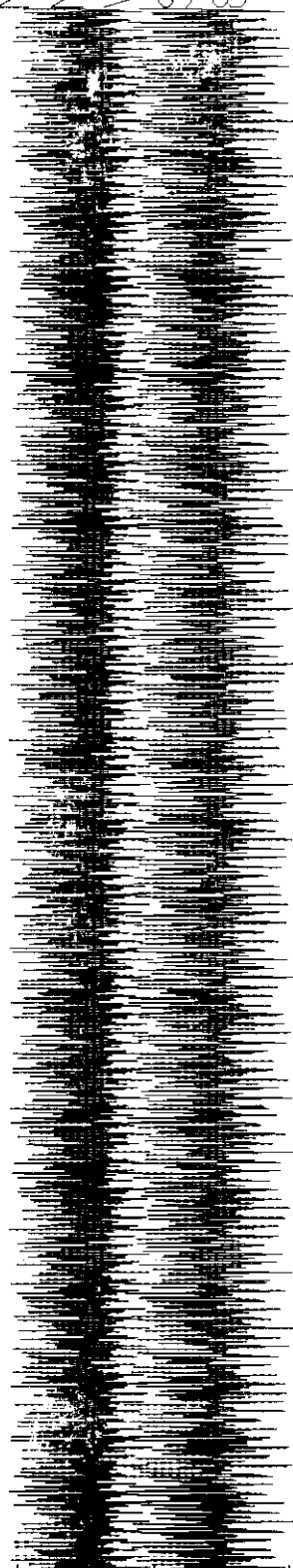
NFT = 0.

VRF 1.00

SYP 68.9

8. GEV

AMP(*10²)



0.00 .40 .81 1.22 1.63 2.04 2.45 2.86 3.27 3.68 4.09

TURN(*10-3)

NUM=39.

86/12/18. 09.35.2
86/12/18. 10.01.3
TC11C FILE 10

FIG.3f